

# Predictions for two-pion correlations for $\sqrt{s}=14$ TeV proton-proton collisions

Tom Humanic  
Ohio State University

# Outline of the talk

- Introduction
- Simple geometric model to give “baseline” predictions for HBT from pp@LHC
- Reality check of model by comparing with Tevatron HBT experiment
- Results of model calculations for  $\sqrt{s}=14$  TeV
- Summary

(work to appear in Phys. Rev. C, or see nucl-th/0612098v2)

An aerial photograph of the Geneva area, showing the city, Lake Geneva, and the surrounding mountains. A large orange oval is drawn over the city, representing the LHC ring. The text "LHC ring in Geneva area" is written in red in the upper right. The text "p+p and Pb+Pb @ LHC" is written in black in the center, enclosed within the orange oval.

LHC ring in  
Geneva area

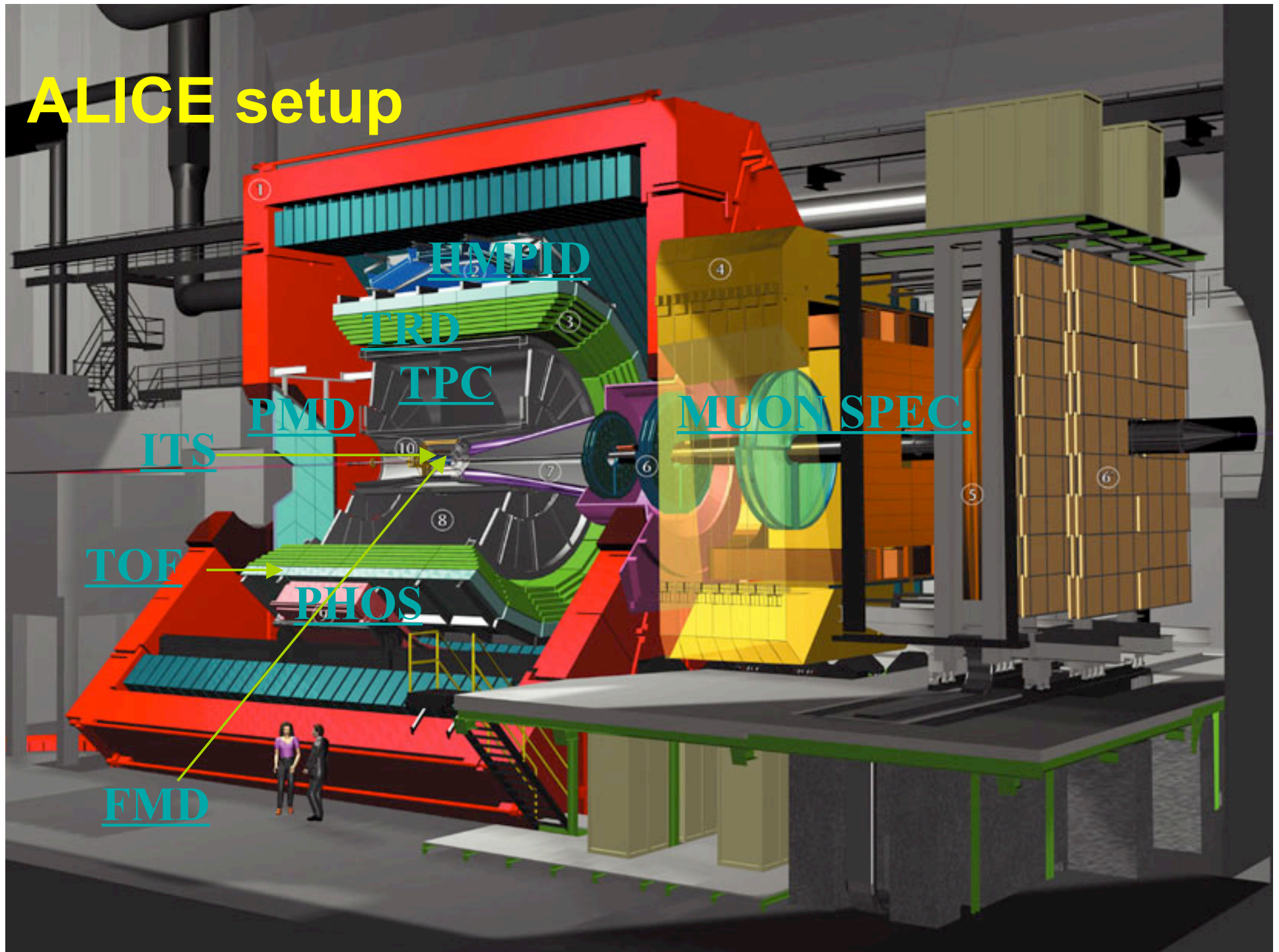
**p+p and Pb+Pb @ LHC**

# CERN Large Hadron Collider (LHC)

- \* Located in Switzerland and France – 27 km circumference ring
- \* Maximum C. M. energies and luminosities of colliding beams:

|                  |  |
|------------------|--|
| proton + proton: | 14 TeV @ $10^{34}$ collisions/(sec*cm <sup>2</sup> )   |
| lead + lead:     | 5.5 ATeV @ $10^{27}$ collisions/(sec*cm <sup>2</sup> ) |
- \* First p-p beam for physics expected by Summer, 2008  
First Pb-Pb beam by ~ end of 2009 (we hope!)
  - better have some interesting p-p physics to do while waiting for Pb-Pb: e.g. HBT, mini-BH, .....
- \* Will be the highest energy particle accelerator in the world!  
(Tevatron presently running at Fermilab has a maximum C.M. energy for p-p of 2 TeV)

# ALICE setup

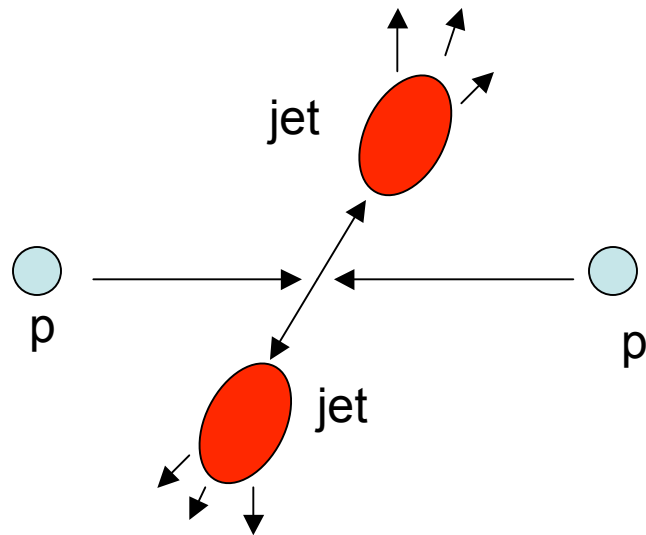


# What do we expect to see from pion HBT with p+p @ LHC?

Jet model for HBT with p+p @ FNAL/LHC

Guy Paic and Piotr Skowronski

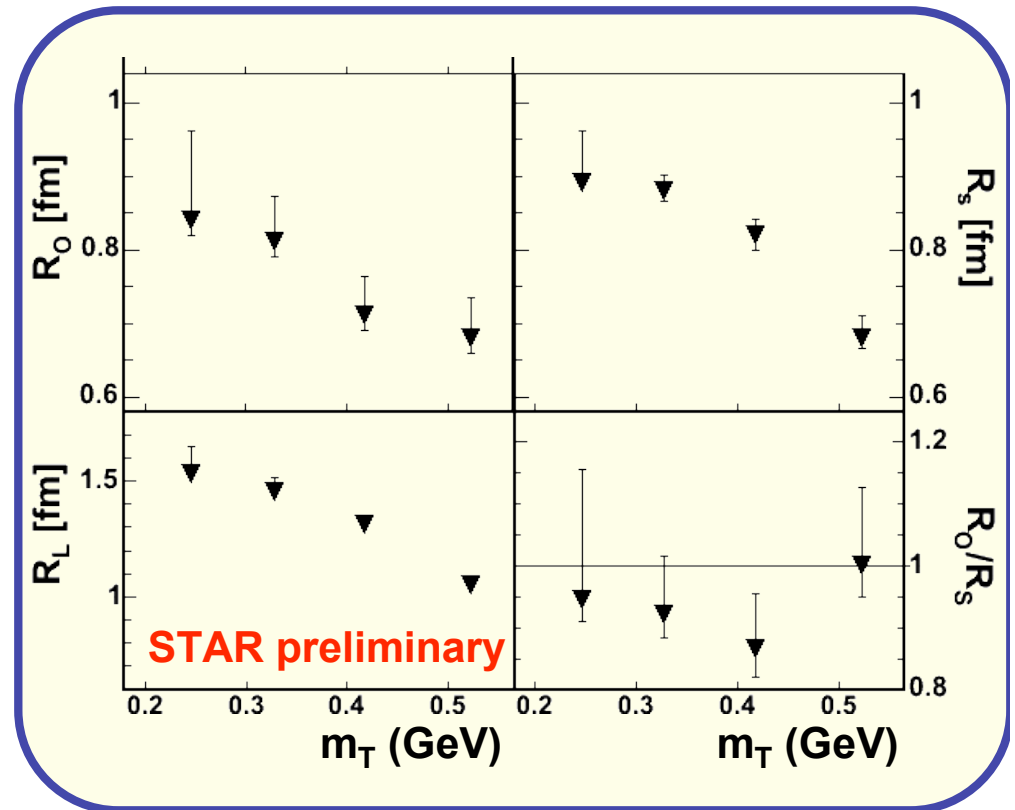
J. Phys. G: Nucl. Part.. Phys. 31 (2005)



Finds  $R$  increases as  $dN/dy$  increases, as seen in FNAL data

Pion HBT with p+p @ STAR

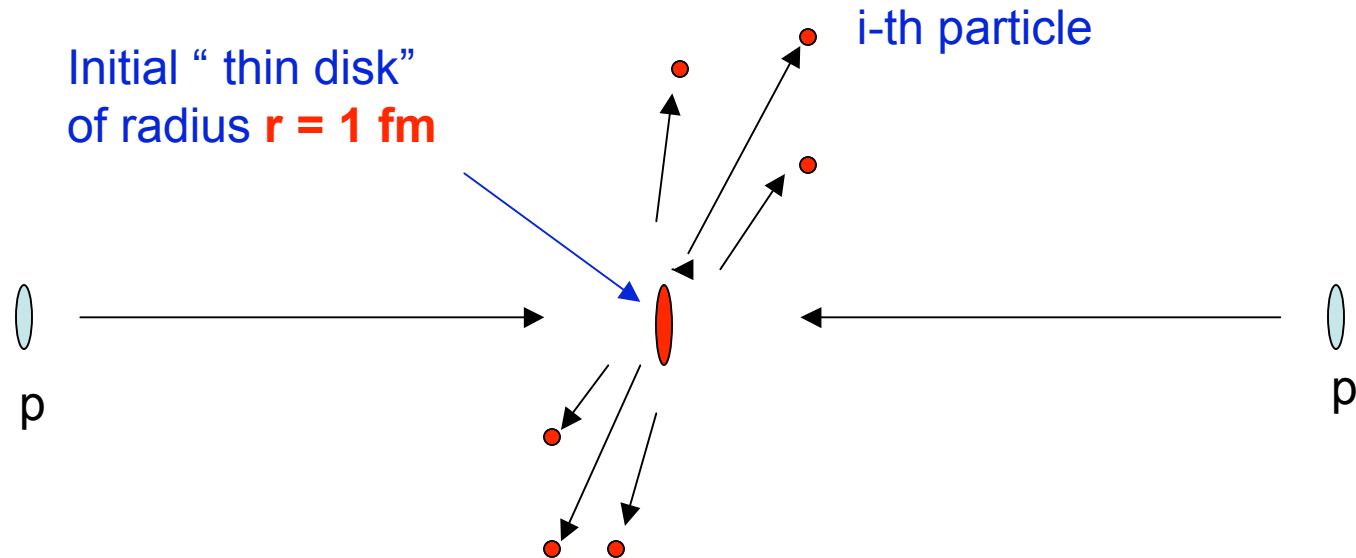
Zbigniew Chajecki QM05



# Goals of the present work

- Use a very simple model to make “baseline predictions” for pion HBT in pp@LHC --> differences between these predictions and LHC data could point to the presence of new physics
- Calculate the 1-d invariant two-pion correlation function  $C(Q_{\text{inv}})$ , where  $Q_{\text{inv}} = |\mathbf{p}_1 - \mathbf{p}_2|$  and  $\mathbf{p}_1$  and  $\mathbf{p}_2$  are pions 4-momenta, to make the predictions simpler to compare with data
- Include final-state hadronic rescattering effects since large hadronic multiplicities (e.g.  $> 300$ ) are possible at the LHC -- concentrate on events with high multiplicity to enhance this effect
- Do a reality check of the model by comparing results with a Tevatron HBT experiment (Experiment E735) --> if the model fails miserably here already, it's time for the junk pile!

# Simple geometric model for HBT from p+p



- \* Assume **all** particles have the same proper time for hadronization,  $\tau$ , so that the hadronization space-time for each particle is given by "causality", i.e.

$$t_i = \tau E_i/m_i ; x_i = x_{oi} + \tau p_{xi}/p_i ; y_i = y_{oi} + \tau p_{yi}/p_i ; z_i = \tau p_{zi}/p_i$$

(similar to Csorgo and Zimanyi, Nucl. Phys. A512 (1990) applied to e<sup>+</sup>-e<sup>-</sup>)

- \* Take into account hadronic rescattering using a full Monte Carlo rescattering calculation



## Other details of the model....

- Use **PYTHIA v.6326** to generate hadrons for 1.8 TeV p-pbar or 14 TeV p+p “minimum bias” events  
“final” hadrons from PYTHIA to use:  $\rightarrow \pi, K, N, \Delta, \Lambda, \omega, \rho, \phi, \eta, \eta'$
- Monte Carlo hadronic rescattering calculation:  
Let hadrons undergo strong binary collisions until the system gets so dilute (since it is expanding) that all collisions cease.  
 $\rightarrow \sigma(i,j)$  from Prakash, etc..  
Record the time, mass, position, and momentum of each hadron when it no longer scatters.  $\rightarrow$  freezeout condition.
- Calculate  $C(Q_{inv}) \sim N_{real}(Q_{inv})/N_{back}(Q_{inv})$  by binning symmetrized pairs of pions assuming plane waves in  $N_{real}$  to put in HBT correlations (usual method).
- Fit Gaussian (Tevatron) or more general function (LHC) to  $C(Q_{inv})$  to extract parameters **R** and  **$\lambda$** , **or** **R**,  **$\lambda$** , **B**, and  **$\alpha$**  :  
 $C(Q_{inv}) = 1 + \lambda \exp(-R^2 Q_{inv}^2)$  **or**  $C(Q_{inv}) = 1 + \lambda \cos(B Q_{inv}^2) \exp(-R^\alpha Q_{inv}^\alpha)$
- Carry out calculations for several  **$\tau$**  values to see effect on HBT --  
expect the smaller values of  **$\tau$**  to have the largest rescattering effects

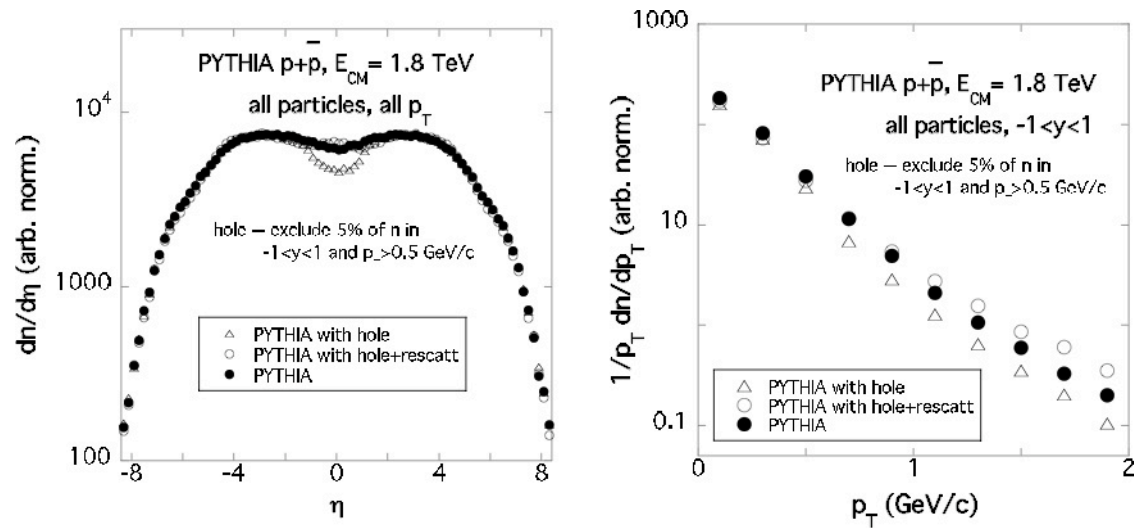
# How long does it take to collect a “reasonable” data sample of, for example, $\pi^+\pi^-$ pairs for events with total mult>300 in a detector at the LHC?

- Assumptions:
  - \* reasonable data sample of  $\pi^+\pi^-$  pairs for HBT:  $\sim 10^6$
  - \* detector: ALICE ITS+TPC ( $\sim$ accept.  $0.1 < p_T, -1 < y < 1$ ; DAQ rate 100Hz)
  - \* 1st-year LHC p-p luminosity @ 14 TeV:  $L \sim 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$
  - \*  $\sim 40\%$  of charged particles reconstructed in an event are  $\pi^\pm$ 's
- From PYTHIA p-p minimum bias run @ 14 TeV
  - \*  $\sigma_{\text{total}} \sim 50 \text{ mb}$ ,  $\sigma(m > 300) = 0.1 \sigma_{\text{total}} \sim 5 \text{ mb}$
  - \* charged hadron multiplicity in ALICE acceptance for  $m > 300$ :  $\sim 50/\text{event}$
- Result:
  - \* events/sec =  $L \sigma(m > 300) \sim 5000 > \text{DAQ rate} \rightarrow 100 \text{ events/sec}$
  - \*  $\pi^+\pi^-$  pairs obtained per event  $\sim (0.4 \cdot 50)^2 / 2 = 200 \rightarrow 20,000 \text{ pairs/sec}$
  - $\rightarrow$  running time to obtain  $10^6$  pairs =  $10^6 / 20,000 = 50 \text{ seconds} \sim 1 \text{ minute}$

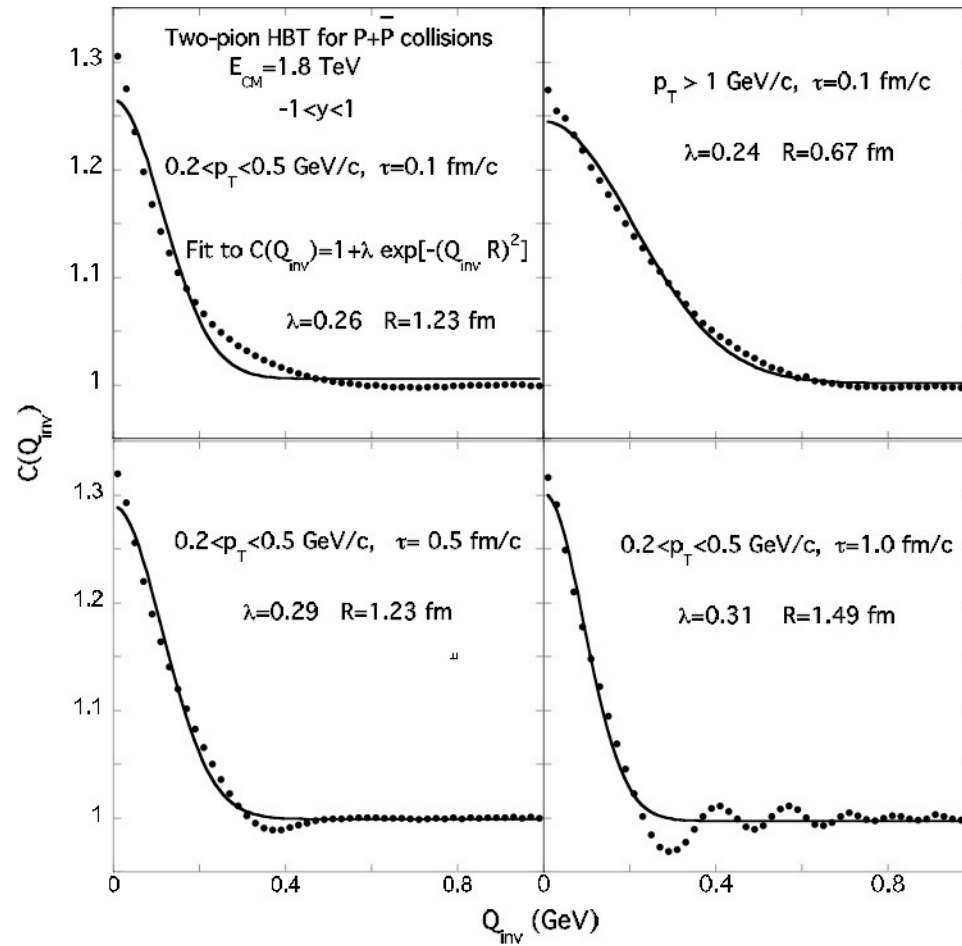
## Compare model predictions with Tevatron data as a reality check on the model

- Compare with Experiment E735 which extracted  $\pi\pi$  HBT @  $\sqrt{s}=1.8$  TeV in p-pbar collisions using a spectrometer (T. Alexopoulos et al., Phys. Rev. D48,1931(1993))
- Make kinematic cuts on  $p_T$  and rapidity to simulate experimental acceptance in the model
- Fit the Gaussian function to  $C(Q_{inv})$  to extract  $R$  and  $\lambda$  from the model since this was the procedure used in the experiment
- Compare model calculations with  $\tau=0.1, 0.5$  and  $1.0$  fm/c to experiment to see if the data favor one of them over the others

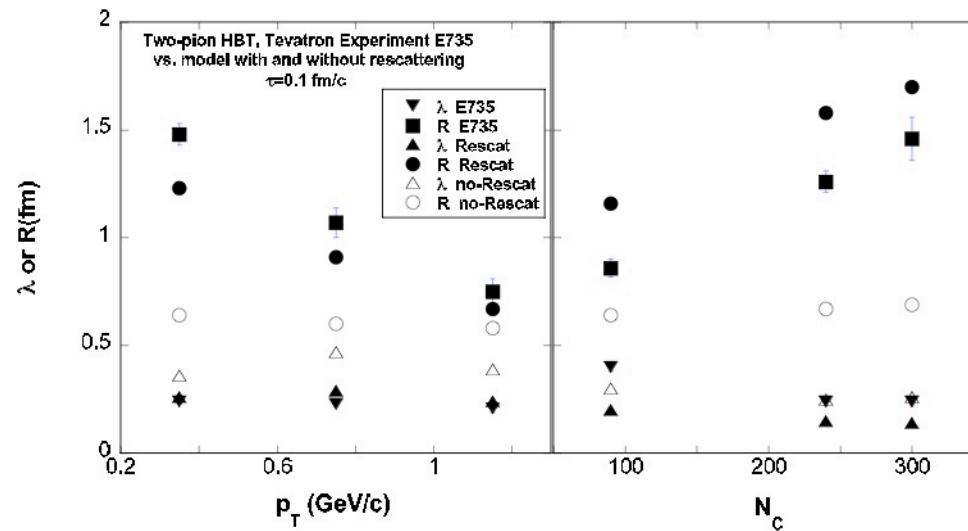
$\eta$  and  $p_T$  distributions from PYTHIA for p-pbar @ 1.8 TeV  
for 1) direct, 2) with “y- $p_T$  hole”, 3) hole+rescatt. ( $\tau=0.1$  fm/c)



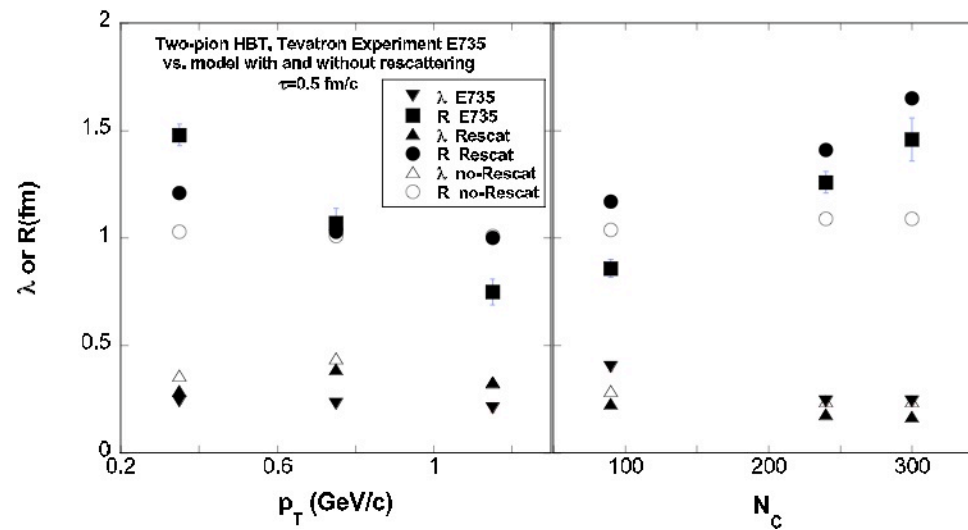
# Sample model 2- $\pi$ correlation functions for $\tau=0.1, 0.5, 1.0$ fm/c for 1.8 TeV p-pbar



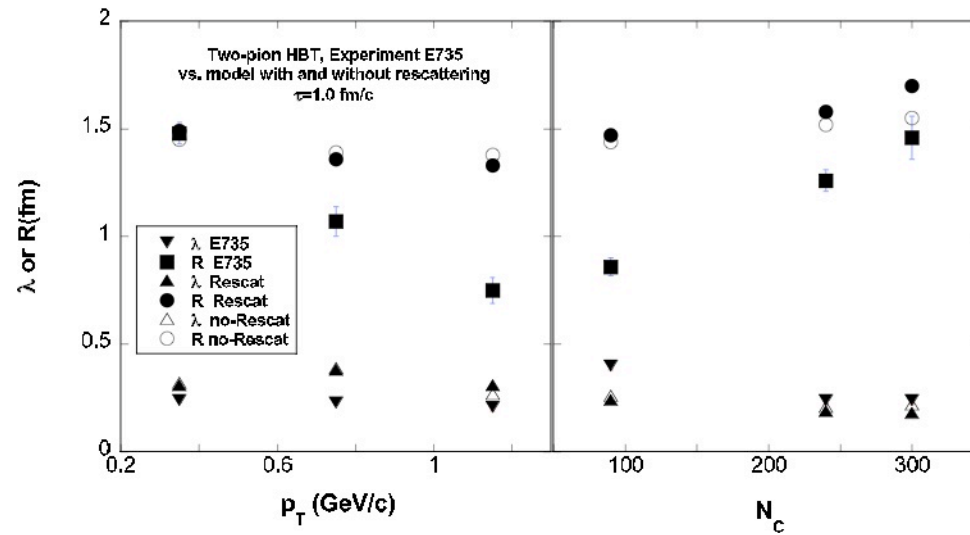
# Comparisons of Gaussian fit parameters between E735 and model for $\tau=0.1$ fm/c



# Comparisons of Gaussian fit parameters between E735 and model for $\tau=0.5$ fm/c



# Comparisons of Gaussian fit parameters between E735 and model for $\tau=1.0$ fm/c





## Summary of results for model comparison with Tevatron experiment

- Model best describes the the  $p_T$  and multiplicity dependences of the E735 Gaussian HBT parameters for the case of  $\tau=0.1$  fm/c with rescattering turned on
- Suggests that hadronization time short in these collisions, i.e.  $\tau \ll 1$  fm/c, and that significant hadronic rescattering effects are present

## Model predictions for LHC p-p collisions at 14 TeV

- Make predictions for  $\tau=0.1$  and  $0.5$  fm/c cases
- Employ same “y- $p_T$  hole” method as used for Tevatron calculations
- Fit more general function to  $C(Q_{inv})$ : (see Csorgo and Zimanyi)

$$C(Q_{inv}) = 1 + \lambda \cos(BQ_{inv}^2) \exp(-R^\alpha Q_{inv}^\alpha)$$

where,

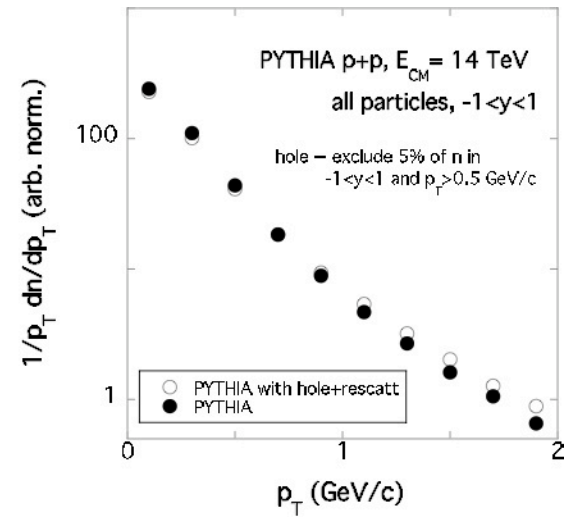
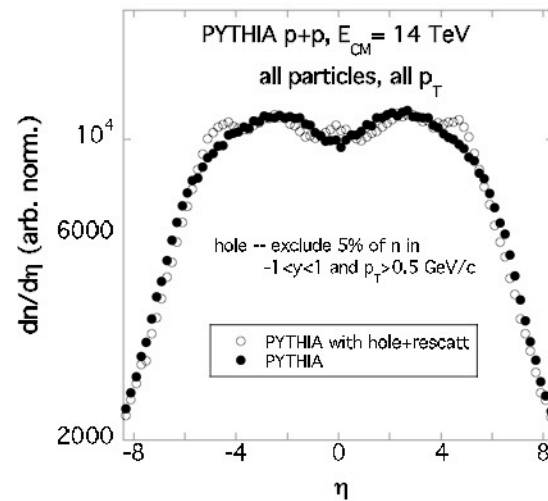
$R$  = “size” parameter

$\lambda$  = “strength” parameter

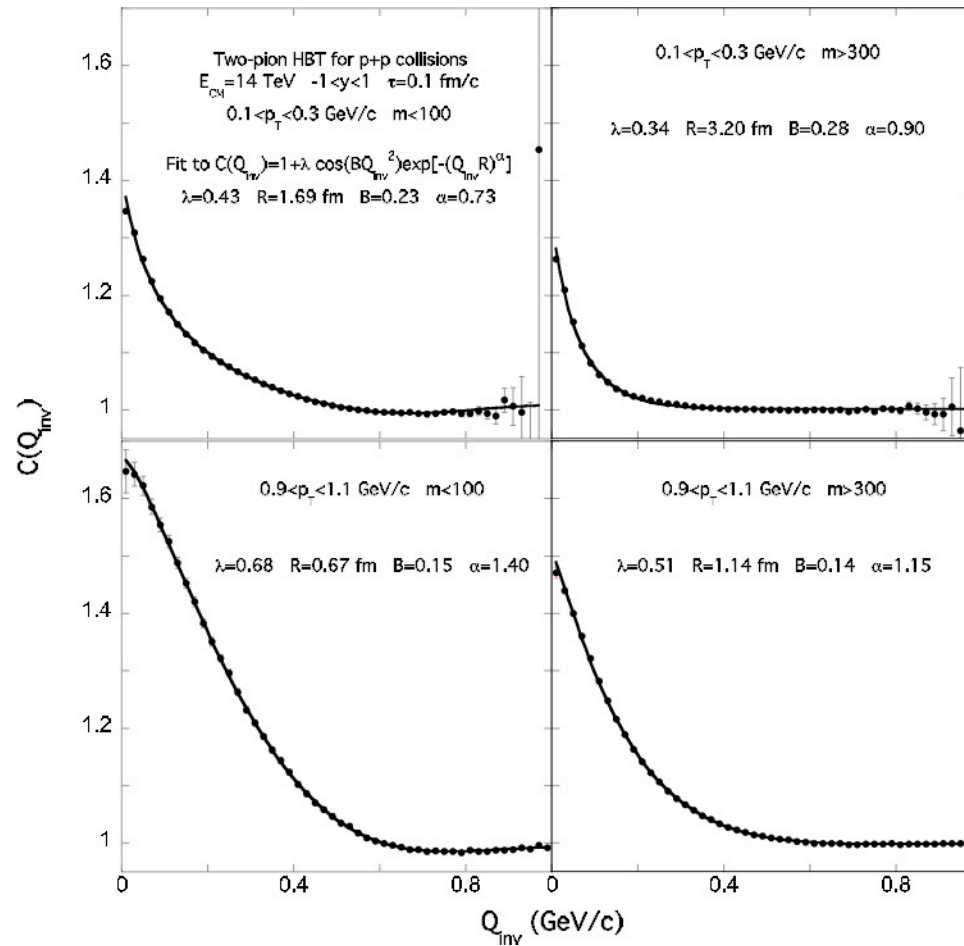
$B$  = “oscillatory” parameter,  $B \sim \tau$  for present model,  
normally not observed for cases where  $R \gg \tau$   
since exp term dominates and quickly damps  
oscillations

$\alpha$  = “degree of function fall-off” parameter

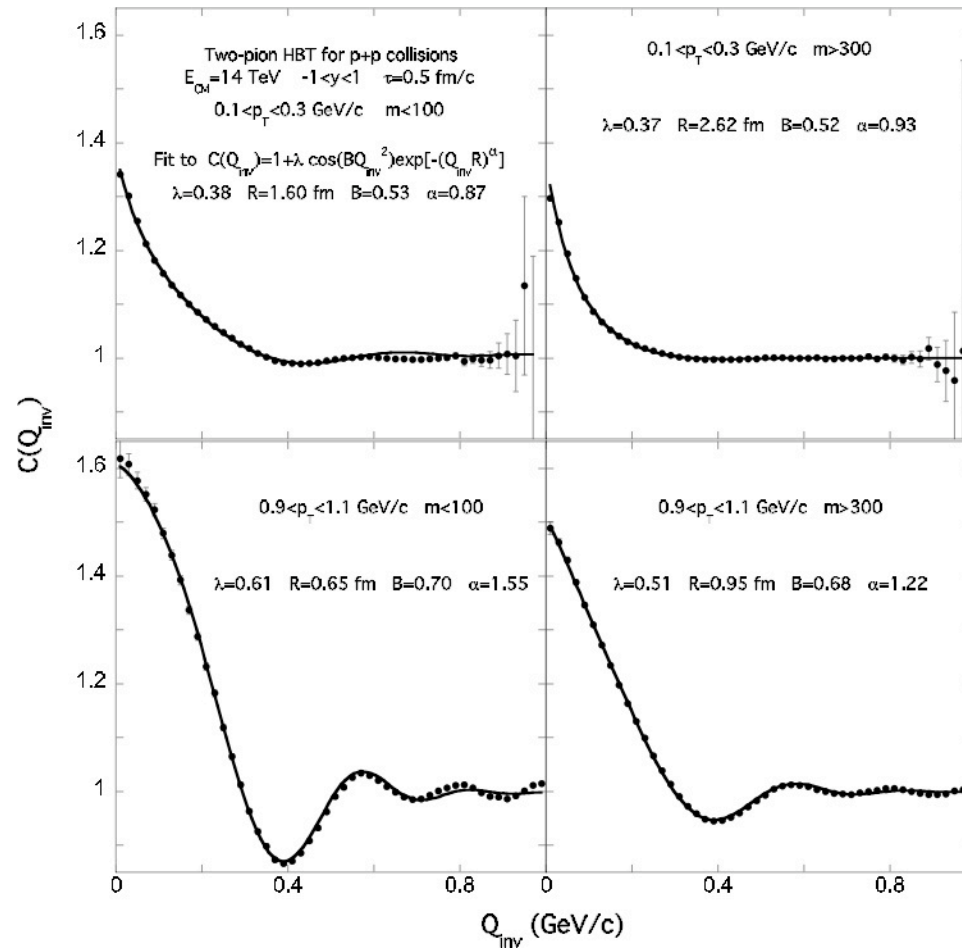
$\eta$  and  $p_T$  distributions from PYTHIA for p-p @ 14 TeV for  
1) direct and 2) hole+rescatt. ( $\tau=0.1$  fm/c)



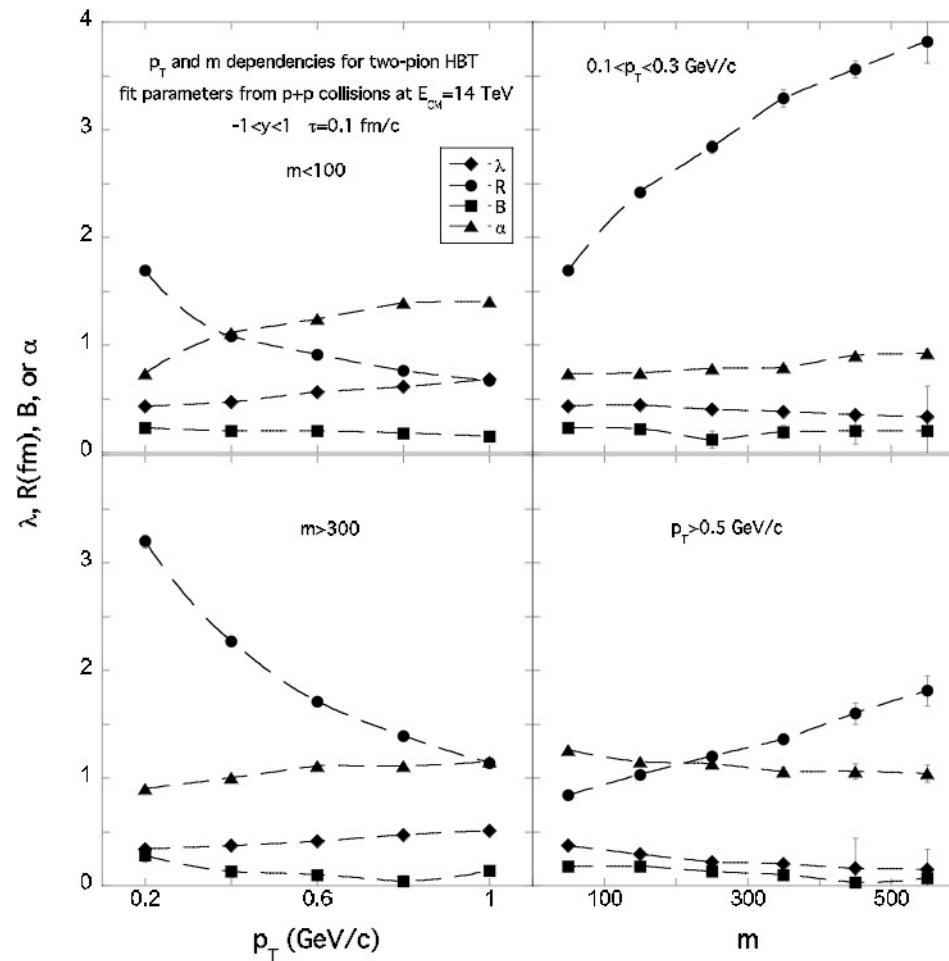
# Sample model 2- $\pi$ correlation functions for $\tau=0.1$ fm/c for 14 TeV p-p with fit to general function



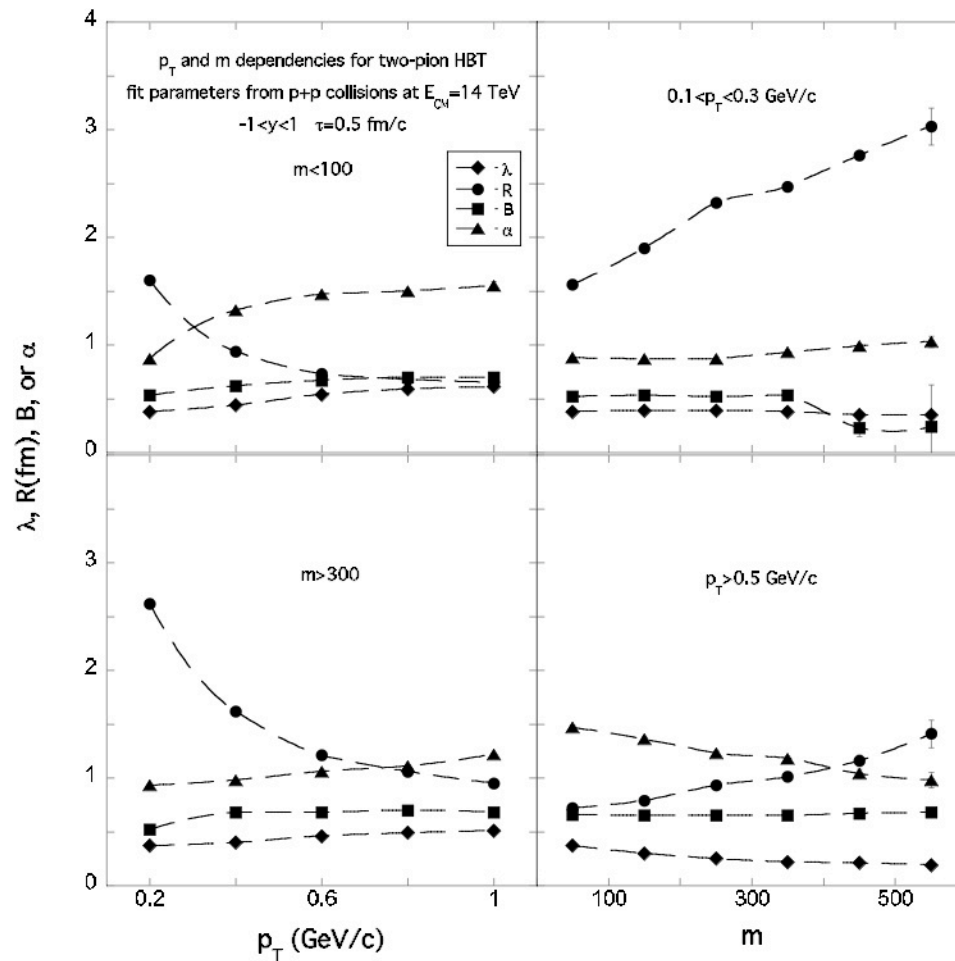
# Sample model 2- $\pi$ correlation functions for $\tau=0.5$ fm/c for 14 TeV p-p with fit to general function



# General fit function parameters versus $p_T$ and multiplicity for model with $\tau=0.1$ fm/c for 14 TeV p-p



# General fit function parameters versus $p_T$ and multiplicity for model with $\tau=0.5$ fm/c for 14 TeV p-p



## Summary of general fit parameter behavior predicted by model for 14 TeV p-p

- **R** -- largest variation for  $\tau=0.1$  fm/c case, can increase by 3x for increasing  $m$  and decrease by 3x for increasing  $p_T$
- **$\lambda$**  -- weak dependencies on kinematical cuts which tend to be opposite those of  $R$ ;  $\lambda < 0.5$  due to presence of long-lived resonances
- **B** -- tends to follow the behavior  $B \sim \tau$ , since noticeable baseline oscillations are seen for the  $\tau=0.5$  fm/c case
- **$\alpha$**  -- similar kinematical dependencies as  $\lambda$ , tends to have values in range  $0.7 < \alpha < 1.5$  for both  $\tau=0.1$  and  $0.5$  fm/c



# Summary

- Within the context of this simple model, results from two-pion HBT @ Tevatron and LHC energies strongly depend on the hadronization proper time,  $\tau$
- Comparison of the model with Tevatron data looks reasonable and favors a short hadronization time,  $\tau \sim 0.1$  fm/c
- Final-state hadronic rescattering effects appear to be observable for  $\tau < 0.5$  fm/c in high-energy p-p and p-pbar collisions
- Significant dependences of the HBT parameters on particle multiplicity and  $p_T$  bin are predicted by the model to be seen for LHC p-p collisions -- these are enhanced for short  $\tau$

